Citation: Woubante G. W. (2017) The Optimization Problem of Product Mix and Linear Programming Applications: Case Study in the Apparel Industry. Open Science Journal 2(2).

Received: 6th January, 2017

Accepted: 20th March, 2017

Published: 19th June, 2017

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Funding: The author(s) received no specific funding for this work

Competing Interests: The author have declared that no competing interests exists.

RESEARCH ARTICLE

The Optimization Problem of Product Mix and Linear Programming Applications: Case Study in the Apparel Industry

Gera Workie Woubante^{*} Bahir Dar University, Bahir Dar, Ethiopia

*Corresponding Author: Gera Workie Woubante: likeredg@gmail.com

Abstract

Industrial development strategy is characterized by the efficient use of resources at every production stage. The analysis and efficient utilization of resources are made sustainable by effective management decision making techniques employed in the industry. A quantitative decision making tool called linear programming can be used for the optimization problem of mix. Understanding the concept behind product the optimization problem of product mix is essential to the success of the industry for meeting customer needs, determining its image, focusing on its core business, and inventory management. Apparel manufacturing firms profit mainly depends on the proper allocation and usage of available production time, material, and labor resources. This paper considers an apparel industrial unit in Ethiopia as a case study. The monthly held resources, product volume, and amount of resources used to produce each unit of product and profit per unit for each product have been collected from the company. The data gathered was used to estimate the parameters of the linear programming model. The model was solved using LINGO 16.0 software. The findings of the study show that the profit of the company can be improved by 59.84%, that is, the total profit of Birr 465,456 per month can be increased to Birr 777,877.3 per month by applying linear programming models if customer orders have to be satisfied. The profit of the company can be improved by 7.22% if the linear programming formulation does not need to consider customer orders.

Keywords: Apparel sector, Linear programming, Lingo, Optimal, Product mix.

Introduction

Companies in the world, including Ethiopia, have faced problems on optimization of production inputs. A company's endurance in a competitive market closely depends on its ability to produce the highest quality products at the lowest possible cost (Kumar, 2010). Ezema and Amakom (2012) emphasized that organizations in the world are challenged by shortages of production inputs and low capacity utilization that can consequently lead to low production outputs. Companies have to create a management style to guide their performances in processing and resource utilization. Apparel manufacturing firm profit is significantly affected by the cost of resources and resource utilization (Arefayne and Pal, 2014). Linear programming is an operational research technique used to allocate optimally production resources for a firm's best practices. It is the most widely used tool (Reeb and Leavengood, 1998) to determine optimal resource utilization. Different products require different amount of production resources having different costs and revenues at different stages of production. Thus, the linear programming problem (LPP) technique will be used to determine the product mix that will maximize the total profit at a specified time. It is the best method for determining an optimal solution among alternatives to meet a specified objective function limited by various constraints and restrictions (Shaheen and Ahmad, 2015). As Reeb and Leavengood (1998) stated, it is a planning process that allocates resources-labor, materials, machines, and capital—in the best possible way so that costs are minimized or profits are maximized. The LPP then becomes a problem of allocating scarce resources to products in a manner such that profits are at a maximum and/or costs are at a minimum (Yahya, 2004). However, managers in companies create gaps in adopting the method to allocate scarce resources among operations and providing quantitative analysis for each production period due to lack of awareness.

An industry consists of a number of product lines, which are groups of items featuring similar characteristics. Together, these product lines comprise the product mix, which is the total assortment of products the company offers. Product mix determination is essential to the success of the industry for a number of important reasons. First, crafting the proper assortment of products provides the best opportunity of meeting customers' needs. The customers come to rely on the industry as their primary resource. By carefully monitoring product mix and seeking feedback from customers, the firm will be able to make adjustments as the needs of customers change over time. Second, it shapes the image of the industry and its brand to maintain consistency in the eyes of the target market. Third, the industry stays focused on its core business. The industry may be tempted to add more product lines in an effort to reach more customers. By doing so, it could be in danger of adding products that appeal only to a fraction of its customer base while alienating the core customers. As a rule, core customers are the ones who provide about 80 percent of the business, so these customers have to be kept in mind when contemplating changes to the product mix. Finally, the industry probably faces limitations regarding the number of products it is able to offer. By focusing on providing the optimum product mix for its customers, it will be able to weed out slow sellers and make room for more appealing items.

In Ethiopia, the apparel sector is considered as one of the priority areas of the government's industrial development strategy (ETIDI, 2014). However, the sector has faced many challenges to determine product mix. It is confronted with inefficient utilization of resources that makes it difficult to ensure the optimal product mix for maximal profit, which would also fulfill customer needs. As noted by Samuel (2012), to modernize the apparel sector, performance was insignificant. Thus, apparel manufacturing companies must adopt operations research techniques to enhance best resource utilization that would result in optimal product mix and total profit. Thus, this paper focuses on product mix determination based on efficient resource utilization for the Ethiopian apparel sector by considering a garment factory in Ethiopia as a case company. The issue addressed here was to determine the product mix for optimal profit with available resources, using the linear programming technique LINGO 16.0, that the case company should produce for men wear: Polo shirt, basic T-shirt, mock neck T-shirt, short pants, and singlet. In line with this, the objective of the study was to suggest linear programming as a decision tool to determine the optimal product mix for maximum profit with available resources in the apparel sector.

Methodology

The data collection procedure was quantitative in nature and relied on faceto-face interviews with members of the management and line supervisors in accordance with existing records and merely amended to finalize the concepts relevant to the resources held and consumed and the production volume of each product in the case company. The relevant information on the amount of resources used per unit of each product during the month is summarized in Table 1.

Table 1: Resources	needed per	unit of	product.
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	Resource	Resource used per unit of products					
Products (T- Shirts and Pants)	Fabrics (Gram)	Threads (Meter)	Labor (Birr)	Overheads (Birr)	Cutting (Min)	Sewing (Min)	Finishing (Min)
Polo T-shirts	315	230	11.6	30.6	1.8	22.7	2
Basic T-shirts	200	110	5	19.1	1.1	5.4	1.3
Mock Neck T- shirts	195	140	6.3	20.1	1.7	10.4	1.9
Singlets	180	100	4.15	16.5	1.1	4.5	1.3

Short Pants 280	200	7.5	37.5	2.6	20.1	2.6
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Source: 2015 Resources used per unit of products of the case apparel company

The ability to use resources (resource utilization) was recorded as the major constraints in the case apparel manufacturing unit. Seven constraints (fabrics, thread, labor, overheads, cutting, sewing, and finishing time) and five costumer orders for T-shirt products have been identified. Out of the resources used by the case apparel company, the major items held and consumed are shown in Table 2.

 Table 2: Average monthly resources held and consumed in quantity/value terms in Birr.

	Resources							
Resource Type	Measurement Unit	Held Value	Consumption Value					
Fabrics	kg	38,665	20,526.871					
Threads	Meter	26,638,120	132,887					
Labor	Birr	1,009,008	590,765					
Overheads	Birr	4,979,414	2,116,525					
Cutting	h	5,770	2,320.42					
Sewing	h	44,505	16,705.7					
Finishing	h	6,195	2,583					

The demand and profit earned from each product during the month for the case apparel company are depicted in Table 3.

	P				
	Polo T- Shirts	Basic T- Shirts	Mock Neck T- shirts	Singlets	Short
Demand	15886	23916	13319	25667	12864
Profit per Unit	4.22	3.62	3.43	3.10	6.75

Table 3: Demand and profit earned.

Model Formulation

In formulating a given decision problem in mathematical form, one should try to comprehensively understand the problem (i.e., formulate a mental model) by carefully reading and re-reading the problem statement. While trying to understand the problem, the decision maker may decide that the model consists of linear relationships representing a firm's objectives and resource constraints. However, the way we approach the problem is the same for a wide variety of decision making problems, and the size and complexity of the problem may differ. An LPP model consists of the following parameters:

Pants

- Decision variables that are mathematical symbols representing levels of activity of an operation.
- > The objective function that is a linear mathematical relationship describing an objective of the firm, in terms of decision variables, that is to be maximized or minimized.
- Constraints that are restrictions placed on the firm by the operating environment situated in linear relationships with the decision variables.
- Parameters/cost coefficients that are numerical coefficients and constants used in the objective function and constraint equations.

Basic Assumptions (Properties) of LPP

Technically, there are five additional requirements of an LPP:

- 1. We assume that conditions of certainty exist; that is, the numbers in the objective and constraints are known with certainty and do not change during the period being studied.
- 2. We also assume that proportionality exists in the objective and constraints. This means that if production of 1 unit of a product uses 3 h of a particular scarce resource, then making 10 units of that product uses 30 h of the resource.
- 3. The third technical assumption deals with additivity, meaning that the total of all activities equals the sum of the individual activities.
- 4. We make the divisibility assumption that solutions need not be in whole numbers (integers). Instead, they are divisible and may take any fractional value.
- 5. Finally, we assume that all answers or variables are nonnegative. Negative values of physical quantities are impossible; we simply cannot produce a negative number of textile products.

Linear Programming Model Formulation Steps

In this section, we consider the steps involved in the mathematical formulation of the problem. LPP is a collection of the objective function, the set of constraints, and the set of nonnegative constraints.

- Step 1: Clearly define the decision variables of the problem, $X = (x_1, x_2, ..., x_n)$.
- Step 2: Write the objective function as a linear combination of the decision variables, Z = f(X).
- Step 3: Formulating the constraints of the problem as a linear combination of the decision variables.

General Form of the Linear Programming Model

In general, if $C = (c_1, c_2, ..., c_n)$ is a tuple of real numbers, then the function f of real variables $X = (x_1, x_2, ..., x_n)$ defined by

$$f(X) = c_1 x_1 + c_2 x_2 + \dots + c_n x_n$$

is known as a linear function. If g is a linear function and $b = (b_1, b_2, ..., b_n)$ is a tuple of real numbers, then g(x) = b is called a linear equation, whereas $g(x) (\leq , \geq)$ b is called a linear inequality. A linear constraint is one that is either a linear equation or a linear inequality. A linear programming problem (LPP) is one which optimizes (maximizes or minimizes) a linear function subject to a finite collection of linear constraints. Formally, any LPP having n decision variables can be written in the following form:

Optimize
$$Z = \sum_{j=1}^{n} C_j X_j$$

Subject to

$$\sum_{i=1}^{m} a_{ij} X_{j} (\leq, =, \geq) b_{i}, i = 1, 2, ..., m$$
$$X_{j} \geq 0, j = 1, 2, ..., n$$

where C_i, a_{ij}, b_i are constants.

Common terminology for the aforementioned linear programming model can now be summarized as follows. The function, being optimized (maximized or minimized), is referred to as the objective function. The restrictions normally are referred to as constraints. The first m constraints (those with a function of all the variables, on the left-hand side) are called functional constraints (or structural constraints). Similarly, the $X_i \ge 0, j = 1, 2, ..., n$ restrictions are called non-negativity constraints (or non-negativity conditions) and the aim is to find the values of the variables X_{i} . Any vector X_{i} , satisfying the constraint of the LPP is called a feasible solution of the problem (Fogiel, 1996; Schulze, 1998; Chinneck, 2000). In this paper, we use the following terminology for the solution. A feasible solution is a solution for which all the constraints are satisfied. An infeasible solution is a solution for which at least one constraint is violated. The problem is to find the values of the decision variables X_i that maximize the objective function Z subject to the m constraints and the non-negativity restriction on the X_i variable. The resulting set of decision variables that maximize the objective function is called the optimal solution.

Results and Discussion

The information collected from the case company in addition to the sales and other operating data was analyzed to provide estimates for LPP model parameters. To set up the model, the first level decision variables on the volume of products to be produced were set.

> x_1 = number of Polo T-shirts x_2 = number of basic T-shirts

 $x_3 =$ number of mock neck T-shirts

- $x_4 =$ number of singlets
- $x_5 =$ number of short pants
- Z = total profit during the month

Now, the linear programming model, maximizing the total profit is:

 $\begin{array}{l} \text{Maximize } Z \ (\text{Birr Profit}) = 5.25 \ x_1 + 4.82 x_2 + 4.85 x_3 + 3.2 x_4 + 6.75 x_5 \\ \text{Subject to} \\ 315 x_1 + 200 x_2 + 195 x_3 + 180 x_4 + 280 x_5 \leq 38,665,000 \ (\text{Fabric}) \\ 230 x_1 + 110 x_2 + 140 x_3 + 100 x_4 + 200 x_5 \leq 26,638,120 \ (\text{Thread}) \\ 12.5 x_1, +5.5 \ x_2 + 6.3 x_3 + 4.25 x_4 + 7.5 x_5 \leq 1,009,008 \ (\text{Labor}) \\ 31 x_1 + 19.1 x_2 + 20.1 x_3 + 37.5 x_4 + 20.1 x_5 \leq 4,979,414 \ (\text{Over heads}) \\ 1.8 x_1 + 1.1 x_2 + 1.7 x_3 + 1.1 x_4 + 2.6 x_5 \leq 346,200 \ (\text{Cutting time}) \\ 22.7 x_1 + 5.4 x_2 + 10.4 x_3 + 4.5 x_4 + 40.1 x_5 \leq 2,670,300 \ (\text{Sewing time}) \\ 2 x_1 + 1.3 x_2 + 1.9 x_3 + 1.3 x_4 + 2.6 x_5 \leq 371,700 \ (\text{Finishing time}) \\ x_1 \geq 15000; \ x_2 \geq 35800; \ x_3 \geq 13500; \ x_4 \geq 12500; \ x_5 \geq 16100 \ (\text{Customer}) \\ \end{array}$

orders)

Model Solution

A powerful linear programming problem solving technique is the simplex method. Among the various software packages, LINGO 16.0 software was used to hold the simplex procedures. The global optimal solution report for this model is as follows.

Objective value:		777877.3
Infeasibilities:		0.000000
Total solver iterations:		2
Elapsed run time seconds	:	0.03
Model class:	LP	
Total variables:	6	
Nonlinear variables:	0	
Integer variables:	0	
Total constraints:	14	
Nonlinear constraints:	0	
Total nonzeros:	47	
Nonlinear nonzeros:	0	

Variable	Value	
Reduced Cost		
Z	777877.3	0.000000
x_1	15000.00	0.000000
x_2	102287.8	0.000000
x_3	13500.00	0.000000
x_4	12500.00	0.000000
x_5	16100.00	0.000000

Row	Slack or Surplu	is Dual Price
1	777877.3	1.000000
2	0.000000	1.000000
3	4091936.	0.000000
4	5576460.	0.000000
5	0.000000	0.8763636
6	1897867.	0.000000
7	128123.4	0.000000
8	1246957.	0.000000
9	124965.8	0.000000
10	0.000000	5.704545
11	66487.82	0.000000
12	0.000000	0.6710909
13	0.000000	0.5245455
14	0.000000	0.3227273

Here, there was a difference between the LPP solutions obtained to satisfy customer orders using LINGO 16.0 and actual production in Table 3. In the former case, the product mix was Polo T-shirts, basic T-shirts, Mock neck T-shirts, singlets, and short pants with volumes of 15,000.00, 102,287.8, 13,500.00, 12,500.00, and 16,100.00 respectively, and with a total profit of Birr 777,877.3 per month upon selling. In the latter case, the product mix was Polo T-shirts, basic T-shirts, mock neck T-shirts, singlets, and short pants with optimal volumes of 15,000.00, 35,800.00, 13,500.00, 12500.00, and 16,100.00 respectively, and with a total profit of Birr 465,456 per month. At optimality, resources consumed by the LINGO 16.0 software result were compared with the customer orders during the month. In this case, the profit of the company could be improved by 59.84 %.

From Table 2, the monthly consumption values of customer orders for each available resource were gathered from the company's records. These consumption values and LPP consumption values are summarized in Table 4. The ratios of monthly consumption of the resources held were calculated to find the percentage usage by each T-shirt style.

Resources H	Resources Held per Month		Monthly	Resources	Percentage	(%)	of
		Consumption		Usage			
			Customer LPP		Customer	LPP	
Туре	Unit	Value	order		order		
Fabrics	Gram	38665000	20,526,871	34573064	53.09	89.42	
Threads	Meter	26,638,120	13,288,700	21061660	49.89	79.07	
Labor	Birr	1,009,008	590,765	1,009,008	58.55	100	

Table 4: Monthly consumption by LPP techniques and customer orderproduction.

Overheads	Birr	4979414	2,116,525	3081547	42.51	61.89
Cutting	Min	346302	139,225	218076.2	40.20	62.97
Sewing	Min	2670336	1,002,344	1423343	37.54	53.30
Finishing	Min	371628	154,982	246734.2	41.70	66.38

The study shows that the LPP resource utilization of fabrics, threads, labor, overheads, cutting, sewing, and finishing can be significantly improved to 89.42%, 79.07%, 100%, 61.89%, 62.97%, 53.30%, and 66.38% respectively. Thus, Figure 1 shows that production based on customer orders lead to inefficient resource utilization since most of the resources are idle.

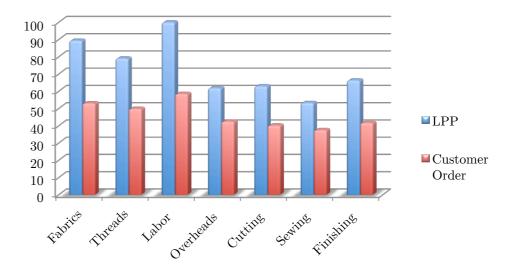


Figure 1: Comparison of customer order and LPP production resources utilization.

Here, an analysis has been made without considering customer orders to develop an LPP model using monthly consumption of resources. The monthly consumption of each resource values are given under the left-hand side column in Table 2, which can be used as required for the constraints.

$$\begin{split} &\text{Maximize } z = 525/100^* \mathrm{X}_1 + 482/100^* \mathrm{X}_2 + 485/100^* \mathrm{X}_3 + 32/10^* \mathrm{X}_4 + 675/100^* \mathrm{X}_5; \\ &\text{Subject to} \\ & & 315^* \mathrm{X}_1 + 200^* \mathrm{X}_2 + 195^* \mathrm{X}_3 + 180^* \mathrm{X}_4 + 280^* \mathrm{X}_5 \leq 20526871; \\ & & 230^* \mathrm{X}_1 + 110^* \mathrm{X}_2 + 140^* \mathrm{X}_3 + 100^* \mathrm{X}_4 + 200^* \mathrm{X}_5 \leq 13288700; \\ & & 125/10^* \mathrm{X}_1 + 5.5 \ ^* \mathrm{X}_2 + 63/10^* \mathrm{X}_3 + 425/100^* \mathrm{X}_4 + 75/10^* \mathrm{X}_5 \leq 590765; \\ & & 31/10^* \mathrm{X}_1 + 191/10^* \mathrm{X}_2 + 201/10 \ ^* \mathrm{X}_3 + 165/10^* \mathrm{X}_4 + 375/10^* \mathrm{X}_5 \leq 2116525; \\ & & 18/10^* \mathrm{X}_1 + 11/10^* \mathrm{X}_2 + 17/10 \ ^* \mathrm{X}_3 + 11/10^* \mathrm{X}_4 + 26/10^* \mathrm{X}_5 \leq 139225; \\ & & 227/10^* \mathrm{X}_1 + 55/10^* \mathrm{X}_2 + 104/10^* \mathrm{X}_3 + 45/10^* \mathrm{X}_4 + 201/10^* \mathrm{X}_5 \leq 1002344; \\ & & 2^* \mathrm{X}_1 + 13/10^* \mathrm{X}_2 + 19/10^* \mathrm{X}_3 + 13/10^* \mathrm{X}_4 + 26/10 \ ^* \mathrm{X}_5 \leq 154982; \\ & & \mathrm{X}_1 \geq 0; \ \mathrm{X}_2 \geq 0; \ \mathrm{X}_3 \geq 0; \ \mathrm{X}_4 \geq 0; \ \mathrm{X}_5 \geq 0. \end{split}$$

The optimal solution values of the decision variables were obtained using the LINGO 16.0 s software. Table 5 shows the monthly product mix of the actual system obtained from the factory and that suggested by the LPP model. These values have been multiplied by their respective unit profits to obtain the profit per month of each product. In this case where customer orders were not considered, the product mix suggested by the LPP model was Polo, basic T-shirt, Mock neck T-shirts, singlets, and short pants at optimal volumes of 0, 330,538.4, 140,265.7, 0, and 28,254.43 respectively with a total profit of Birr 499,058.5 per month. It can be shown then that with the LPP optimal solution, the profit of the company can be improved by 7.22% (499,058.5 – 465,456/465,456) ×100. Adopting operational research techniques in the production decision help the company to improve its objective.

	Profit	Production			
	per Unit	Volume/Mon	nth	Profit (Birr) /Month	
	(Birr)	Customer		Customer	
Product Type		Orders	LPP	Orders	LPP
Polo T-shirts	5.25	15000	0	78,750	0
Basic T-shirts	4.82	35800	68576.43	$172,\!556$	330,538.4
Mock Neck T-					
shirts	4.85	13500	28920.76	65,475	140,265.7
Singlets	3.2	12500	0	40,000	0
Short Pants	6.75	16100	4185.841	108,675	28,254.43
Total Profit/Mor	Total Profit/Month (Birr)				

Table 5: Comparison of customer order production and LPP values.

Conclusion

Ability to use resources (resource utilization) was recorded as the major constraint in the apparel manufacturing industry. The profits comparison between the actual production and production using LPP models show sizeable differences. From this point of view, it can be concluded that the apparel company should use quantitative research methods of linear programming to determine their optimal product mix. Thus, it will be possible to obtain the following results:

- ▶ The profit of the company can be improved by 59.84% (from Birr 465,456 per month to Birr 777,877.3 per month).
- Denying customer orders and adopting the LPP solution provides only three types of products but the profit of the company can be improved by 7.22% (from Birr 465,456 per month to Birr 499,058.5 per month).

➤ Use of an operational research technique in the production time horizon helps the company to improve its objective.

References

- Arefayne, D., & Pal, A. (2014). Productivity Improvement through Lean Manufacturing Tools: A Case Study on Ethiopian Garment Industry. International Journal of Engineering Research & Technology (IJERT), 3 (9), 1037–1045.
- ETIDI. (2014). Textile Industry Development in Ethiopia. An Overview of Facts and Opportunities, Addis Ababa, Ethiopia.
- Ezema, B.I and Amakoml, U. (2012). Optimizing Profit with the Linear Programming Model: A Focus on Golden Plastic Industry Limited, Enugu, Nigeria. Interdisciplinary Journal of Research in Business, 2 (2), 37–49.
- Kumar, V. (2010). JIT Based Quality Management: Concepts and Implications in Indian Context. International Journal of Engineering Science and Technology, 2 (1), 40–50.
- Reeb, J. and Leavengood, S. (1998). Using the Simplex Method to Solve Linear Programming Maximization Problems. Oregon State University, Extension Service
- Samuel, S. (2012). Investigation on the Effect of Supply Chain Integration on Ethiopian Garment Industry's Performance. A Thesis Submitted to the Department of Management. Addis Ababa University, Addis Ababa, Ethiopia.
- Shaheen, S. and Ahmad, T. (2015). Linear Programming Based Optimum Resource Utilization for Manufacturing of Electronic Toys. International Research Journal of Engineering and Technology (IRJET), 2 (1), 261–264
- Yahya W. B. (2004). Determination of Optimum Product Mix at Minimum Raw Material Cost, Using Linear programming. Nigeria Journal of Pure and Applied Sciences, 19, 1712–1721.